

CALCULUS: Graphical, Numerical, Algebraic by Finney, Demana, Watts and Kennedy
Chapter 3: Derivatives Graphs of the Derivative of a function

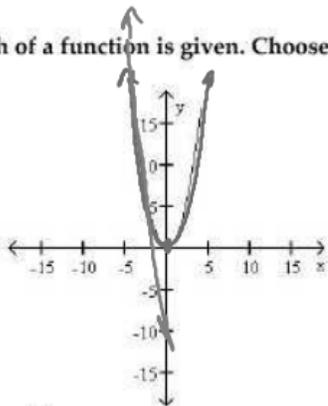
What you'll Learn About

- How to graph the derivative from the original function
- How to graph the function from the derivative

*graph of f'
below
x-axis*

The graph of a function is given. Choose the answer that represents the graph of its derivative.

1)

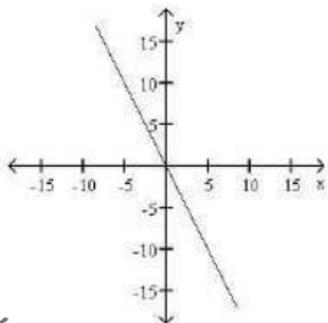


Left
 $(-\infty, 0)$ $f'(x) < 0$ (slope is neg)

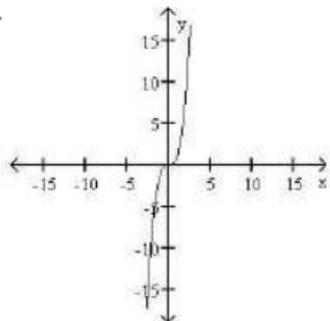
Right
 $(0, \infty)$ $f'(x) > 0$ (slope is +)

f' graph above the x-axis

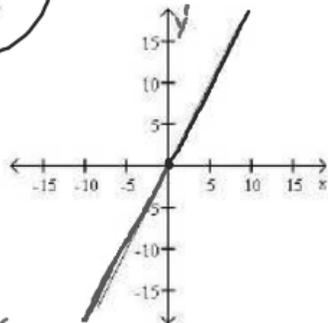
A)



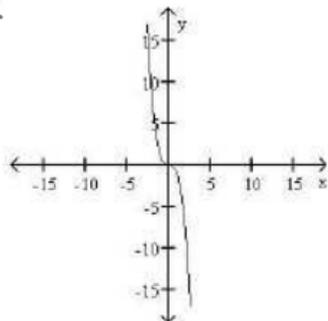
~~X~~



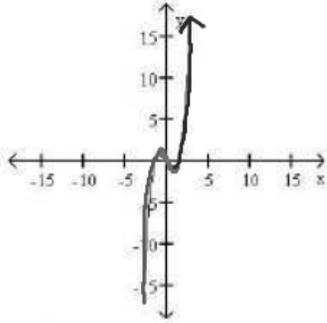
B)



~~X~~

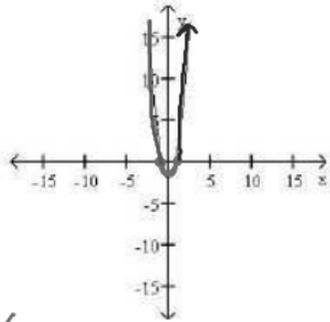


2)

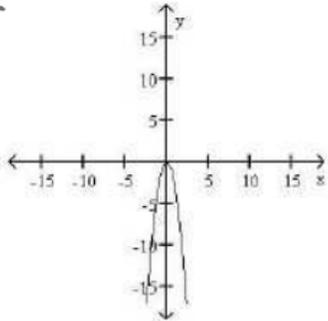


$x \leq -1$ $f'(x) = 0$ (Horizontal Tangent / Slope = 0)
 $x \geq 1$ $-f'(x)$ graph x-int at $x = -1$
 $x = 1$
 $(-\infty, -1)$ $f'(x) > 0$ (f has pos. slope)
 $-f'(x)$ graph above x-axis

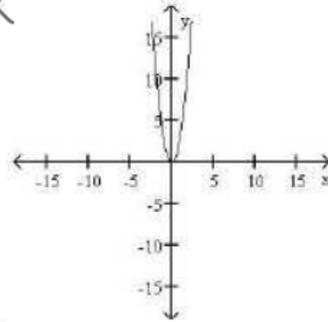
A)



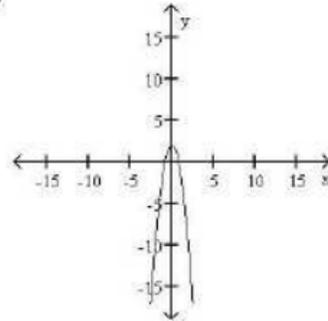
~~C~~

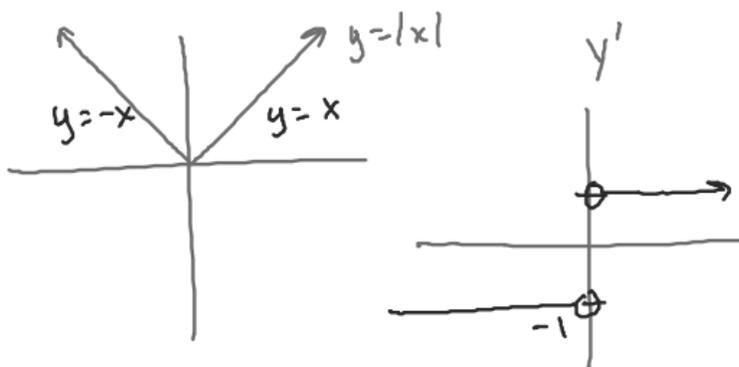
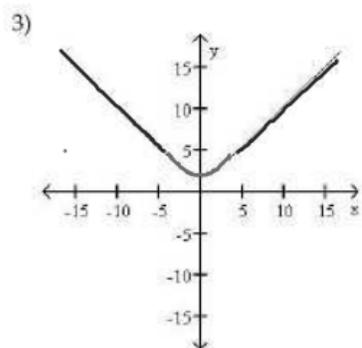


~~B~~

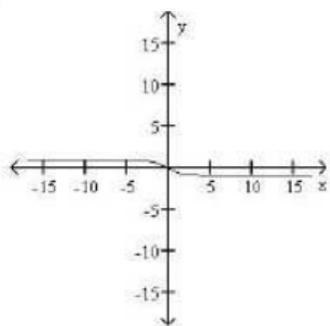


D)

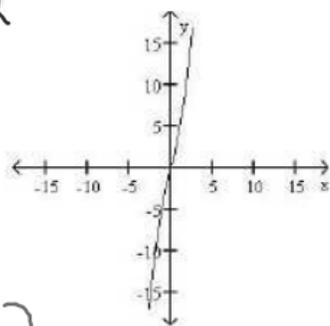




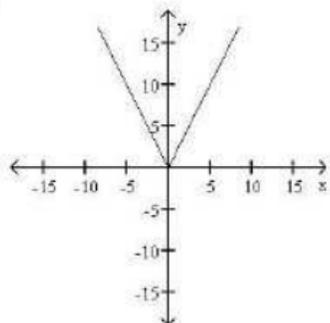
A)



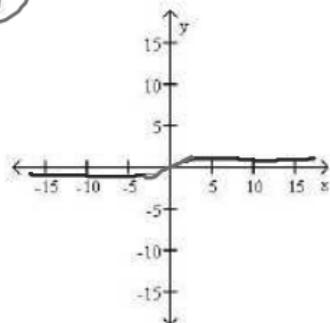
~~B)~~



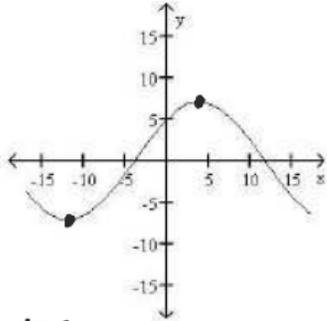
C)



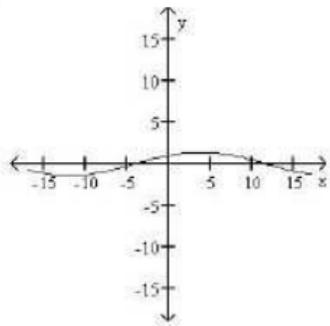
D)



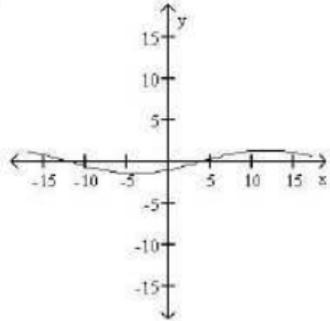
4)



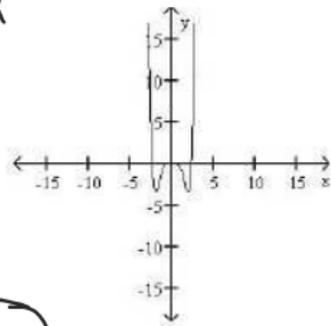
~~X~~



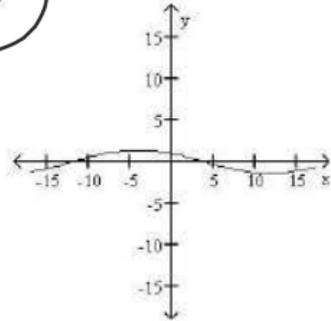
C)



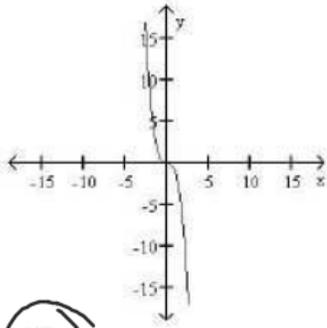
~~X~~



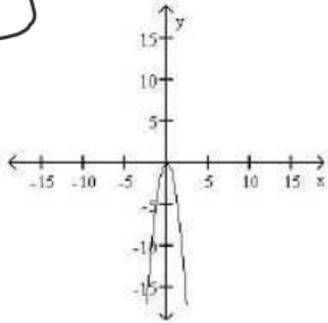
D)



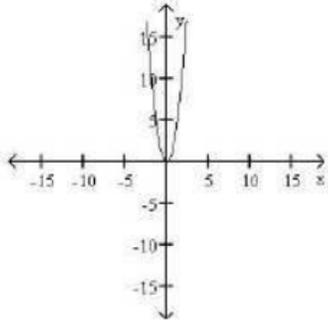
5)



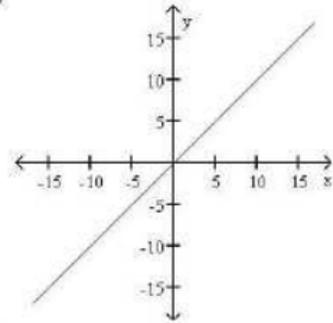
A)



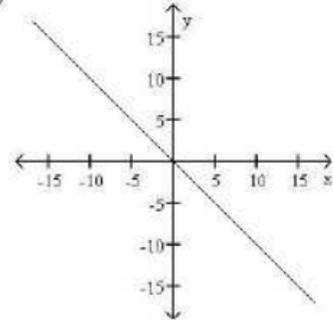
C)



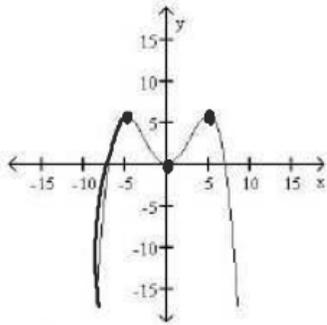
B)



D)

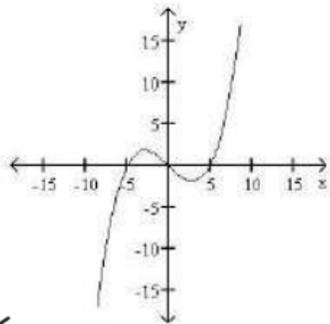


6)

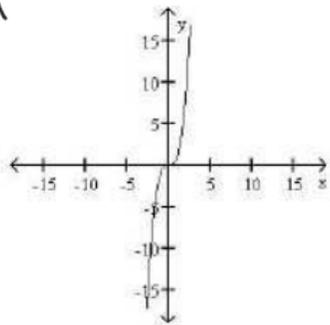


x-int: $x = -4, 0, 6$

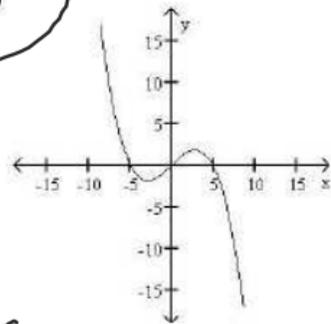
A)



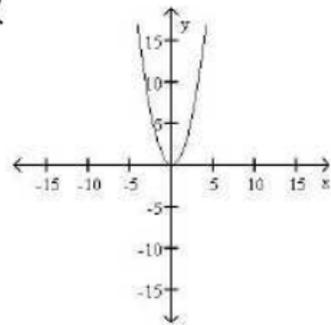
~~X~~



B)



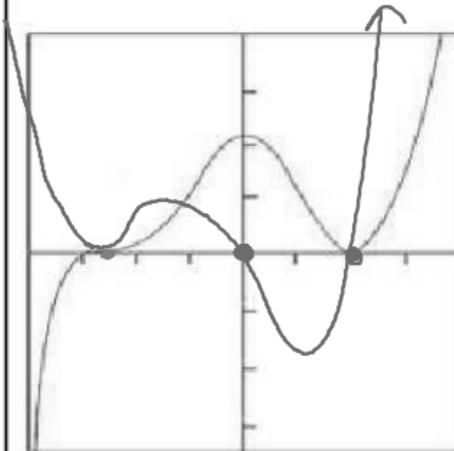
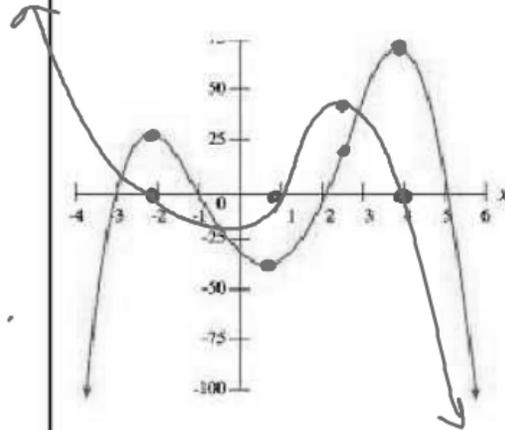
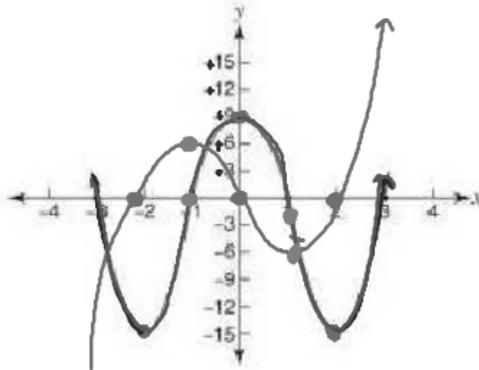
~~X~~



Slope of the original is the steepest $f'(x)$ should have a max or min

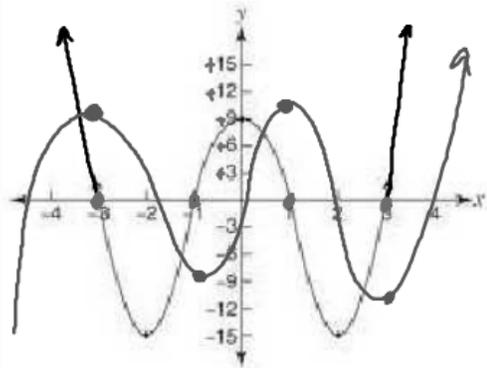
Sketch $f'(x)$ on the same coordinate plane as the given graph of $f(x)$

Max/Min on $f(x)$
 $-f'(x)$ x-int



f' above
 $-f$ inc
 f' below
 $-f$ dec

Sketch $f(x)$ on the same coordinate plane as the given graph of $f'(x)$



$(-\infty, -3)$ f' above x-axis
 f increasing

x-int of f' are
max/min on f

